DSP BASED SPACE VECTOR PWM FOR THREE-LEVEL INVERTER WITH DC-LINK VOLTAGE BALANCING

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ABSTRACT: This paper describes a new PWM method for three-level inverter considering DC-link capacitor balancing problem. Each voltage vector on space vector plane is classified in relation to charging discharging action of DC capacitors and a new modulation method is suggested based on the voltage vector selection principle. The algorithm is implemented on Motorola DSP 56000 and tested with 7.5 KVA prototype three-level transistor inverter. The effectiveness of suggested PWM method is verified by the experimental results.

I. INTRODUCTION

Nowadays three-level PWM inverter is believed to be promising in high power/high voltage AC drives above 4500V where there is no solution with single switching element. It is well known that the three-level inverter has advantages such that the blocking voltage of each switch is clamped to the half of DC-link voltage and the output voltage and current waveform contain low harmonics compared to conventional two-level inverter for the same switching frequency. Various PWM techniques for the three-level inverter have been studied[2-6] since Akira Nabe proposed the topology by the name of NPC inverter in 1981[1]. Such techniques which are regarded as an extension of the conventional two-level PWM include dipole modulation, harmonics elimination, space vector PWM and so forth. So far, however, little attention has been paid to DC-link capacitor voltage balancing problem which is inherent in the three-level inverter topology. It is required that the two DC-link capacitor voltages (E_u and E_l in Fig. 1) should be maintained balanced condition to guarantee the true three-level operation throughout the whole output voltage range. If it is violated, the output contains even order harmonics including second order which is fatal in AC drives.

In the following sections, DC-link voltage balancing problem is discussed in detail and two kinds of solutions are suggested; one is closed loop method with sensing circuitry the other is open loop method without any sensing. Especially the open loop method is described in detail and a new modulation technique is suggested for it. The new PWM is based on the synchronous space vector PWM with constant carrier frequency that controls the time integral of output vol-
tage to have circular trajectory in d-q plane and whereby neutral point can be controlled to maintain unbiased to upper or lower DC-link rail. Various experiments are also given to verify effectiveness of suggested PWM method.

II. DC-link capacitor voltage balancing problem

Fig. 1 shows the circuit diagram of three-level inverter and Fig. 2 shows equivalent simplified three-level inverter for respective two different switch states considering load connections to describe the voltage balancing problem of the capacitor. The two capacitors of Fig. 1 are replaced by a single one in Fig. 2 by adding together. The figure represents that the motor load is connected across $E_u$ and $E_l$, respectively. The two case is completely equivalent at the load side providing that $E_u$ is equal to $E_l$. As it is shown, the neutral terminal is not of a rigid voltage source but of a capacitor. Thus it is not guaranteed that $E_u$ and $E_l$ maintain equal because $E_l$ goes larger in case (a) and goes smaller in case (b) according to charging discharging action. Either of the two states can’t sustain even for one or two periods of the inverter frequency before the potential of the central terminal reaches to that of upper or lower rail by charging or discharging. If this situation happens, it is impossible to operate the inverter any longer. Furthermore, if the capacitor which has the voltage rating less than $V_{DC}$ is adapted, all would burn out. If the two states are continued for $T_u$ and $T_l$, respectively in average, then $E_u$ and $E_l$ approaches $T_u \cdot V_{DC}/(T_u + T_l)$ and $T_l \cdot V_{DC}/(T_u + T_l)$, respectively, with some time constant which is a function of

![Figure 1](image1.png)

![Figure 2](image2.png)

Fig. 2 Load connections of (a) charging,
(b) discharging vector

![Figure 3](image3.png)

Fig. 3 Phase voltage and spectrum
(a)(b) under balanced condition
(c)(d) under unbalanced condition ($E_u/E_l=1.7$)
capacity of DC capacitor and the load. So the capacitor voltage balancing problem is closely related to choice of vector and its duration. The capacitor balancing problem can also be regarded as load balancing problem.

Fig. 3(a) and (b) show the phase voltage waveform and its spectrum for balanced condition while (c) and (d) shows the case for unbalanced condition when \( E_u/E_0 = 1.7 \). The output voltage waveform of the unbalanced case is seriously distorted compared to the balanced case. As shown in the frequency spectrum, the second harmonic does not exist in the balanced condition whereas it appears in the unbalanced condition. The second harmonic which is proportional to unbalanced voltage cause serious problems in AC drives such as current harmonics, torque pulsation and power losses.

III. Space vector of three-level inverter

Space vector notation is very useful tool to understand capacitor voltage balancing problem because vector notation shows load connection directly. The output of three-level inverter has 27 different vectors as shown Fig. 4. We identify the voltage vectors such as [+] , [−0] and so on. For example, in case of [+] , SU1, SU2, SV2, SV3, SW3, and SW4 in Fig. 1 are in ON and the others in OFF states. Thus the output terminal U, V, and W has the potential of \( +V_{DC}/2, 0 \), and \( -V_{DC}/2 \), respectively, and the corresponding load connection is shown in Fig. 5(b). The voltage vector can be classified into some categories according to its magnitude. Such categories are zero vector(ZV), small vector(SV), medium vector(MV), and large vector(LV) as listed in Table 1. The SV group is subdivided into upper small vector(UV) and lower small vector(LV) again. Each group has its own role concerning charging or discharging action. The ZV and the LV has no effect on charging discharging because the load is not connected between neutral point and the upper/lower rail. The MV is somewhat effective on improving voltage unbalance. The SV is the most effective for the balancing because UV has charging action and LV has discharging action. Thus special care must be paid in the selection between UV and LV. We can control the neutral point voltage using SV group either by closed loop or by open loop control.

![Space vectors of three-level inverter](image)

**Table 1** Classification of space vectors

<table>
<thead>
<tr>
<th>Vector</th>
<th>(0,0), [++]</th>
<th>[−0], [0+], [0−], [00]</th>
</tr>
</thead>
<tbody>
<tr>
<td>ZV</td>
<td>[−+], [−0], [−0], [−0], [−0]</td>
<td></td>
</tr>
<tr>
<td>SV</td>
<td>[+0], [+0], [0+], [0+], [0+], [0+]</td>
<td></td>
</tr>
<tr>
<td>USV</td>
<td>[−0], [−0], [−0], [−0], [−0], [−0]</td>
<td></td>
</tr>
<tr>
<td>LSV</td>
<td>[+0], [+0], [+0], [+0], [+0], [+0]</td>
<td></td>
</tr>
<tr>
<td>MV</td>
<td>[−0], [−0], [−0], [−0], [−0], [−0]</td>
<td></td>
</tr>
<tr>
<td>LV</td>
<td>[−0], [−0], [−0], [−0], [−0], [−0]</td>
<td></td>
</tr>
</tbody>
</table>

![Representative vectors and their load connections](image)
IV. PROPOSED PWM TECHNIQUES

Fig. 7 shows the different switch state in the first quadrant of d-q plane. Here, \( V_n \) is the sampled value of the reference voltage vector rotating with angular speed \( \omega \) at certain instant. If \( V_n \) falls into the triangle established by the straight lines that interconnect the voltage vectors \( V_1, V_2, \) and \( V_3 \), the duration of each vector can be calculated by the following relations.

\[
V_n \cdot T = V_1 \cdot t_1 + V_2 \cdot t_2 + V_3 \cdot t_3 \tag{1}
\]

\[
T = t_1 + t_2 + t_3 \tag{2}
\]

where \( T \) is sampling time of reference voltage vector.

i) Neutral point control by closed loop

Fig. 6 roughly shows closed loop control method with voltage sensor together with PWM algorithm. The vector classifier judges whether the present vector is SV and whether neutral point potential is in acceptable range. If the neutral point potential is close to that of the upper rail beyond boundary, the PWM controller decrease the USV duration by \( \Delta T \) and increase the LSV duration by \( \Delta T \). In this case it is necessary to compromise between dynamics and stability in considering \( \Delta T \).

![Fig. 6 Neutral point control by closed loop](image)

ii) Neutral point control by open loop

Although we do not adapt closed loop control, voltage balancing can be achieved if special PWM technique is employed to select USV and LSV evenly. The PWM method must be synchronous one such as dipole modulation, harmonics elimination or synchronous space vector PWM (alias star modulation) because the load should be distributed evenly without feedback. In general, synchronous space vector PWM is preferred to others because relatively good waveforms can be obtained in spite of its simple configuration. If PWM algorithm is implemented on 16bit microprocessor, the calculation error can be under \( 10^{-5} \). The error is mainly due to driver and device mismatch. However it is small enough in practice and is not accumulated. Thus the total unbalancing is not so large that the system could cause no serious problems.

![Fig. 7 Selection of vectors and their sequence](image)
i) Region A1

In this region, the vector sequence is given in the order \( \text{LSV}[0-0] - \text{USV}[+00] - \text{ZV}[000] \). Voltage balancing is satisfied because LSV and USV are selected alternatively for the interval time \( T \).

ii) Region A2

The vector sequence is given \( \text{LSV}[0-0] - \text{MV}[+-0] - \text{UW} [+00] \) in this region. Because LSV and USV are selected alternatively during time \( T \), voltage balancing is satisfied. Furthermore MV influences in such a way to improve the voltage unbalance.

iii) Region A3

The vector sequence is given \( \text{LSV}[0-0] - \text{MV}[-0+] - \text{LV} [++-] \). Although only LSV is used, there is little problem in voltage balancing, because \( V_n \) will move into the region A4 in \( T \) or in \( 2T \).

In this manner we chose the voltage vectors used in the PWM and determined their sequence satisfying in capacitor voltage balancing as in Fig. 3.

VI. Experiments

The implementation of the proposed PWM method is established on 7.5 KVA prototype transistor 3-level inverter controlled by Motorola DSP 56000. The PWM control algorithm is constructed with assembly language and operates in real time. The computation takes about 230 \( \mu \text{sec} \) which is enough to operate the inverter in real time because the \( T \) is larger than 4 \( \mu \text{sec} \). In this case the switching frequency for each device corresponds about 500Hz which is usual value in several MVA GTO inverter. The experimental results are shown for two different magnitudes of the output as represented in Fig. 8 and 9. The symmetry of the each voltage in Fig.8 and Fig.9 shows that DC-link capacitor voltage balancing is satisfied fairly good. Fig. 10 shows harmonic current factor (HCF) for various \( q \) by computer analysis where \( q \) is the number of division per cycle of the inverter frequency or

\[
q = \frac{2\pi}{T \omega}
\]

The \( T \) is sampling time of reference voltage vector and \( \omega \) is the angular speed of the inverter output voltage.

The bold line represents selected PWM pattern to suppress HCF under 2.5%.

V. CONCLUSION

This paper pointed out the seriousness of the voltage unbalancing problem inherently resides in the three-level topology. All the space vectors of three-level inverter are classified concerning voltage balancing. Two solutions to it are suggested, one is closed loop and the other open loop control. Especially, a new PWM technique is suggested based on space vector as a method of the open loop control. The experiment showed that the suggested PWM techniques is suitable to high power GTO three-level inverter satisfying capacitor voltage balancing.

REFERENCES

Fig. 8 When $f_{\text{inv}} = 20\text{Hz}$, $m$ (modulation index) = 0.3 and $q = 84$

(a) trajectory of time integral of output voltage
(b) pole voltage (100V, 10msec/div)
(c) line-line voltage (100V, 10msec/div)
(d) phase voltage (100V, 10msec/div)
(e) line current (10A, 10msec/div)
(f) spectrum
Fig. 9 When $f_{\text{inv}} = 50\text{Hz}$, $m = 0.8$ and $q = 24$
(a) trajectory of time integral of output voltage
(b) pole voltage (100V, 20msec/div)
(c) line-line voltage (100V, 20msec/div)
(d) phase voltage (100V, 20msec/div)
(e) line current (10A, 20msec/div)
(f) spectrum

Fig. 10 HCF for various $q$