Neutron Rietveld analysis for optimized CaMgSi$_2$O$_6$:Eu$^{2+}$ and its luminescent properties

Won Bin Im

Department of Materials Science and Engineering, Korea Advanced Institute of Science and Technology, Daejeon 305-701, Republic of Korea

Yong-Il Kim

Korea Research Institute of Standards and Science, Yuseong, Daejeon 305-600, Republic of Korea

Jong Hyuk Kang and Duk Young Jeon

Department of Materials Science and Engineering, Korea Advanced Institute of Science and Technology, Daejeon 305-701, Republic of Korea

Ha Kyun Jung and Kyeong Youl Jung

Advanced Materials Division, Korea Research Institute of Chemical Technology, Yuseong-gu, Daejeon 305-600, Republic of Korea

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We optimized synthesis conditions of blue-emitting CaMgSi$_2$O$_6$:Eu$^{2+}$ (CMS:Eu$^{2+}$) with conventional solid-state reaction and successfully determined structure parameters by Rietveld refinement method with neutron powder diffraction data. The final weighted R-factor $R_{wp}$ was 6.42% and the goodness-of-fit indicator $S (= R_{wp}/R_e)$ was 1.34. The refined lattice parameters of CMS:Eu$^{2+}$ were $a = 9.7472(3)$ Å, $b = 8.9394(2)$ Å, and $c = 5.2484(1)$ Å. The $\beta$ angle was 105.87(1)$^\circ$. The concentration quenching process was observed, and the critical quenching concentration of Eu$^{2+}$ in CMS:Eu$^{2+}$ was about 0.01 mol and critical transfer distance was calculated as 12 Å. With the help of the Rietveld refinement and Dexter theory, the critical transfer distance was also calculated as 27 Å. In addition, the dominant multipolar interaction of CMS:Eu$^{2+}$ was investigated from the relationship between the emission intensity per activator concentration and activator concentration. The dipole–dipole interaction was a dominant energy transfer mechanism of electric multipolar character of CMS:Eu$^{2+}$.

I. INTRODUCTION

BaMgAl$_{10}$O$_{17}$:Eu$^{2+}$ (BAM) is an efficiency blue phosphor for plasma display panels (PDPs) because of its high luminescence under vacuum ultraviolet (VUV) excitation. However, the luminance decrease and color shift of this phosphor that occur during the baking process are well known problems. The thermal degradation of the phosphor that occur during the baking process is a particularly serious problem for manufacturing of PDP panels. It has been reported that the thermal degradation of BAM is probably related to the change of either the valence of Eu$^{2+}$ to Eu$^{3+}$ or its crystal structure (β-alumina), which has an open layer in the crystal. 1–3

Based on this information, CaMgSi$_2$O$_6$:Eu$^{2+}$ (CMS:Eu$^{2+}$) has been proposed as a way to overcome the drawbacks of BAM because it is more stable under the baking process and has relatively good photoluminescence (PL) properties under VUV excitation. 2,3 However, the PL intensity of CMS:Eu$^{2+}$ excited by 147 nm sources is weaker than that of BAM, and the study on crystal structure of CMS:Eu$^{2+}$ also has not been done sufficiently. To obtain CMS:Eu$^{2+}$ phosphor of high luminescence efficiency, we have optimized it in terms of factors such as activator concentration, gas flow rates, and SiO$_2$ ratios. Since, in 147 nm excitation, the excitation wavelength is shorter than absorption edge of the host lattice, the VUV spectrum does not excite an activator directly. In addition, the VUV spectrum is very well absorbed into the CMS crystal so its penetration depth into the phosphor particle is very small. For this reason, CMS:Eu$^{2+}$ phosphor must have a property of high energy transfer from host lattice to activators. 1

Furthermore, the precise crystal structural information of CMS:Eu$^{2+}$ is necessary to improve its optical property. In addition to this, it is highly desirable to initiate a detailed electronic structure study. The blue emission band of CMS:Eu$^{2+}$ is mainly caused by the Eu$^{2+}$ luminescent center, which may have replaced Ca$^{2+}$ sites
partially in the CMS compound. In particular, it is very important to determine the quantitative amount of Eu\(^{2+}\) in the crystal lattice because the amount of Eu\(^{2+}\) doped into the crystal lattice is directly related to optical properties of CMS:Eu\(^{2+}\); thus an accurate description of the location and population degree of Eu\(^{2+}\) ions in CMS:Eu\(^{2+}\) is essential.

In this study, we optimized blue-emitting CMS:Eu\(^{2+}\) and performed the crystal structural refinement of CMS:Eu\(^{2+}\) by means of Rietveld refinement using neutron powder diffraction data. In addition, we investigated the mechanism of energy transfer in Eu\(^{2+}\) of critical concentration and Dexter’s theory for energy transfer.

II. EXPERIMENTAL

Powder samples of CMS:Eu\(^{2+}\) were prepared by conventional solid-state reaction. To synthesize CMS:Eu\(^{2+}\) phosphor, CaCO\(_3\) (Kojundo, Japan, 99.99%), MgO (Aldrich 99.99%), SiO\(_2\) (Kojundo, Japan, 99.99%), and EuF\(_3\) (Aldrich 99.99 %) were used as raw materials. Small quantities of NH\(_4\)F were added as a flux. The raw materials were mixed in a ball mill mixer for 12 h and heated subsequently at 1150 and 1200 °C in a reducing atmosphere of H\(_2\) (5%) and N\(_2\) (95%) for 3 h, respectively. PL spectra were obtained at room temperature by scanning wavelength region from 350 to 600 nm under an excitation of 147 nm radiation from a deuterium lamp. The excitation spectrum in VUV region was corrected by sodium salicylate.

Neutron powder diffraction data were collected over scattering angles ranging from 0° to 160° using 1.8348 Å neutron on high resolution powder diffractometer (HRPD) at the Hanaro Center of the Korea Atomic Energy Research Institute in Daejeon, Korea. The General Structure Analysis System (GSAS) program was used to do the structural refinement.\(^4\) A pseudo-Voigt function was chosen as the best trial profile function among many possible profile functions in GSAS.\(^5\) The neutron scattering lengths for Ca, Mg, Si, and O atoms are 0.4700, 0.5375, 0.4149, and 0.5803 \(\times 10^{-12}\) cm, respectively.

III. RESULTS AND DISCUSSION

A. Optimization of Ca\(_{0.99}\)Mg\(_{2.2}\)O\(_6\):0.01Eu\(^{2+}\) phosphor for high luminance

The dependence of emission intensity on Eu concentration is presented in Fig. 1. We investigated the PL intensity of the CMS:Eu\(^{2+}\) with varying Eu concentrations from 0.005 to 0.3 mol. It was found that the optimum concentration of Eu for CMS:Eu\(^{2+}\) was 0.01 mol. From more than 0.1 mol of activator concentration, a significant drop in relative emission intensity was observed, due to concentration quenching.

Figure 2 shows the relative PL intensity of CMS:Eu\(^{2+}\) phosphors as a function of gas flow rates with the concentration of activator Eu fixed at 0.01 mol. As shown in Fig. 2, the gas flow rate was optimized at 0.2 l/min. In this case, the body color of the phosphor powders appears white. As gas flow rate increases over 0.2 l/min, the crystallinity of the host material became poor due to strong reducing atmosphere. In addition, light yellow color phosphor powders were obtained when gas flow rate was more than 0.6 l/min because the host lattice was reduced strongly. In contrast, when weak reducing atmosphere was introduced, the Eu\(^{3+}\) ions was not easily reduced to Eu\(^{2+}\) ions. It was found from these results that the PL intensity of CMS:Eu\(^{2+}\) was very easily affected by synthesis conditions.

We also performed experiments with varying SiO\(_2\) mole ratios to improve the PL intensity of CMS:Eu\(^{2+}\)
phosphor. According to Ropp’s report, a small amount of excess SiO2 is used in synthesis of inorganic phosphor materials to ensure a complete solid-state reaction among the reacting species and to avoid the presence of strongly absorbing cationic species in the final product. However, if the amount of SiO2 is beyond a critical value, the PL intensity may decrease considerably due to the increase of unreacted SiO2 per unit area. For this reason, it is essential to quantitatively determine the quantity of SiO2 phase in inorganic phosphors. Figure 3 shows relative PL intensity depending upon SiO2 mol ratios. The stoichiometric ratio of CaO:Mg:SiO2 is 1:1:2 for CMS:Eu2+. However, the highest brightness can be obtained when 0.2 mol excess SiO2 is introduced in the starting mixture of raw materials. For the 0.2 mol excess SiO2, PL intensity increased by about 10% in comparison with that of stoichiometric composition. It is well known that in the case of Zn2SiO4:Mn2+, the highest brightness can be obtained with excess SiO2. Above 0.2 mol excess SiO2, PL intensity decreased as much as 25% due to increase of unreacted SiO2 per unit area.

B. Structural refinement of optimized Ca0.99MgSi2.2O6:0.01Eu2+ phosphor

The structural refinement was carried out for the optimized CMS:Eu2+ phosphor. A reasonable approximation of the actual crystal structure as a starting model is required to do the crystal structural refinement. The starting structural model for CMS:Eu2+ was built with the crystallographic data reported by Levien et al. This was based on the C12/c1 space group. Although the convergence was achieved by the initial structural refinement, some unknown diffraction peaks remained unaccounted for within the experimental profile. Considering the starting materials and experimental variables such as pressure, temperature, and environment atmosphere, CaO, SiO2, MgO, EuO, CaSiO3, etc., might be proposed to exist within CMS:Eu2+ samples. Of these possible phases, the remaining reflection peaks could be indexed satisfactorily to SiO2 (cristobalite). Consequently, the synthesized sample was composed of CMS:Eu2+ and SiO2 phases. The initial structure model of SiO2 as a secondary phase was based on the crystallographic data of SiO2, with the space group P412121.

The disorder of Eu2+ ions was considered after refinement with two-phase model for the synthesized sample. When Eu2+ ions are incorporated into the crystal structure of CMS, Eu2+ ions may substitute for all cationic sites, Ca2+, Mg2+, and Si4+. However, considering their respective ionic radii and allowed oxygen-coordination number (n)—Mg2+ (0.72 Å, n = 6), Si4+ (0.26 Å, n = 4), Ca2+ (1.12 Å, n = 8) and Eu2+ (1.25 Å, n = 8)—it is difficult for Eu2+ ions to substitute for Mg2+ or Si4+ ions. Therefore, the structural refinement proceeded under the assumption that Eu2+ ions substituted for only Ca2+ ions. Consequently, the Rietveld refinement was carried out under the assumption that Eu2+ ions substitute only for Ca2+ ions. The occupancies of Eu2+ and Ca2+ sites were constrained so that both sites were fully occupied, and the total occupancy of Eu2+ and Ca2+ ions was maintained to be unity. The temperature factors of the atoms to occupy the two sites were set to be equal. Through the preliminary structural refinement, the background, scale factor, lattice parameters, profile parameters, asymmetrical parameters, atomic positions, and isotropic atomic displacements, etc., for all atoms, were optimized. After this structural refinement had converged, the occupation factors were refined with the constraints of occupation and thermal factors.

Figure 4 shows the structural refinement patterns for the mixture model of CMS:Eu2+ and SiO2 phases. The final weighted R-factor Rwp was 6.42%, and the goodness-of-fit indicator S ( = Rwp/Rr) was 1.34. Table I listed the refined structural parameters of CMS:Eu2+ obtained from the above structural refinement. The occupations of Eu atoms occupying the Ca sites are 0.013 and totally substitute for 1.3% of the Ca atoms. The weight fractions of CMS:Eu2+ and SiO2 based on the scale factors were 96.45(2)% and 3.55(2)%, respectively. The refined lattice parameters of CMS:Eu2+ were a = 9.7472(3) Å, b = 8.9394(2) Å, c = 5.2484(1) Å, and β = 105.87(1)°.

C. Photoluminescence properties of Ca0.99MgSi2.2O6:0.01Eu2+ phosphor

Figure 5 shows the excitation and PL spectra of the optimized CMS:Eu2+ under a 147 nm excitation. In the excitation spectrum, direct excitation bands appeared from 250 to 320 nm. Its emission was measured at 447 nm. The emission band corresponds to the transition from the 4f5Sd excited state to the 4f7 ground state of a
Eu\textsuperscript{2+} ion.\textsuperscript{11} The obtained CIE color coordinates of the synthesized CMS:Eu\textsuperscript{2+} were \(x = 0.148\), \(y = 0.0389\).

To understand the energy transfer mechanism of CMS:Eu\textsuperscript{2+}, it is useful to know the critical distance \((R_c)\) for energy transfer between the sensitizer and activator. In this study, we used Dexter’s formula,\textsuperscript{12} which represents restricted transfer of electric dipole–dipole interaction since we are dealing with allowed electric–dipole transitions in the case of Eu\textsuperscript{2+}. The probability of transfer dipole–dipole interaction has been given by Dexter as

\[
R_c^2 = 0.63 \times 10^{28} \frac{4.8 \times 10^{-16} \cdot P}{E^4 \cdot SO}. \tag{1}
\]

Here \(P\) is the oscillator strength of the Eu\textsuperscript{2+} ion, \(E\) is the energy of maximum spectral overlap, and SO is the spectral overlap integral,\textsuperscript{13} which represents the product of normalized spectral shapes of emission and excitation. The values of \(E\) and SO can be derived from the spectral data in Fig. 5. For \(P\) corresponding to the broad \(4f^7 \rightarrow 4f^65d\) absorption band, a value of \(10^{-2}\) is taken.\textsuperscript{13,14} The values of \(E\) and SO are obtained from the spectra, which are 2.97 eV and \(1.1 \times 10^{-2}\) eV\textsuperscript{−1} (0.5 × height × width = 0.5 × 0.12 × 0.19), respectively. From Eq. (1), the value of \(R_c\) for the energy transfer in CMS:Eu\textsuperscript{2+} was calculated as 12 Å.

In addition, it is possible to calculate the \(R_c\) from the data of concentration quenching and number of cations present in the unit cell. In this case, the critical distance is equal to the average shortest distance between the nearest activator ions corresponding to the critical concentration \((X_c)\).\textsuperscript{15} The critical distance from data concentration quenching is represented as

\[
R_c = 2 \left( \frac{3V}{4\pi X_c N} \right)^{1/3}. \tag{2}
\]

### TABLE I. Structural parameters of CMS:Eu\textsuperscript{2+} obtained from the structural refinement using neutron powder diffraction data taken at room temperature. The symbols, \(g\) and \(U_{iso}\), represent the occupation factor and isotropic thermal parameter, respectively. The numbers in parentheses are the estimated standard deviations of the last significant figure.

<table>
<thead>
<tr>
<th>Atom</th>
<th>Site</th>
<th>(x)</th>
<th>(y)</th>
<th>(z)</th>
<th>(g)</th>
<th>(100 U_{iso}/\text{Å}^2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CaMgSi\textsubscript{2}O\textsubscript{6}:Eu\textsuperscript{2+}</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ca</td>
<td>4e</td>
<td>0.0</td>
<td>0.3003(2)</td>
<td>0.25</td>
<td>0.987(1)a</td>
<td>1.69(3)b</td>
</tr>
<tr>
<td>Eu</td>
<td>4e</td>
<td>0.0</td>
<td>0.3003(2)</td>
<td>0.25</td>
<td>0.013(1)</td>
<td>1.69(3)</td>
</tr>
<tr>
<td>Mg</td>
<td>4e</td>
<td>0.0</td>
<td>0.9087(2)</td>
<td>0.25</td>
<td>1.0</td>
<td>0.68(2)</td>
</tr>
<tr>
<td>Si</td>
<td>8f</td>
<td>0.2858(2)</td>
<td>0.0934(2)</td>
<td>0.2283(3)</td>
<td>1.0</td>
<td>0.45(2)</td>
</tr>
<tr>
<td>O</td>
<td>8f</td>
<td>0.1158(1)</td>
<td>0.0868(2)</td>
<td>0.1415(2)</td>
<td>1.0</td>
<td>0.78(3)</td>
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<tr>
<td>O</td>
<td>8f</td>
<td>0.3619(2)</td>
<td>0.2409(3)</td>
<td>0.3182(3)</td>
<td>1.0</td>
<td>1.05(2)</td>
</tr>
<tr>
<td>O</td>
<td>8</td>
<td>0.3508(3)</td>
<td>0.0171(2)</td>
<td>0.9932(3)</td>
<td>1.0</td>
<td>0.71(3)</td>
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<tr>
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<td>C12/c1 (No. 15) and (Z = 4)</td>
<td>(a = 9.7472(3)), (b = 8.9394(2)) Å and (c = 5.2484(1)) Å; (\beta = 105.87(1)^\circ)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SiO\textsubscript{2}</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Si</td>
<td>4a</td>
<td>0.2191(23)b</td>
<td>0.2191(23)</td>
<td>0.0</td>
<td>1.0</td>
<td>2.86(31)</td>
</tr>
<tr>
<td>O</td>
<td>8b</td>
<td>0.2389(32)</td>
<td>0.0841(24)</td>
<td>0.2000(37)</td>
<td>1.0</td>
<td>2.84(42)</td>
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<tr>
<td>Space group:</td>
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<td>(a = b = 4.9882(22)) Å and (c = 6.937(39)) Å</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Weight fraction</td>
<td></td>
<td>CaMgSi\textsubscript{2}O\textsubscript{6}:Eu\textsuperscript{2+}</td>
<td>96.45(2)%</td>
<td>SiO\textsubscript{2}</td>
<td>3.55(2)%</td>
<td></td>
</tr>
</tbody>
</table>

\(\textsuperscript{a}\text{Constraint on occupancy: } g(\text{Ca}) + g(\text{Eu}) = 1.0.\)

\(\textsuperscript{b}\text{Constraint on isotropic thermal factor: } U_{iso}(\text{Ca}) = U_{iso}(\text{Eu}).\)
Taking the values of $V$, $N$, and $X_c (V = abc \sin\beta = 439.93 \text{ Å}, N = 4, X_c = 0.01$, shown in Table I and Fig. 1), the critical transfer distance of Eu$^{2+}$ in CMS:Eu$^{2+}$ turned out to be 27 Å. From the calculated results mentioned above, the value of $R_c$ is not well matched with the $R_c$ obtained from the Dexter formula because the critical distance value using the critical concentration data involves the whole possible interaction between host lattice and activator. However, the critical distance value obtained using spectra overlap data considered dipole–dipole interaction. Furthermore, in the case of VUV excitation, the energy transfer process from the host lattice to the activator could play a significant role in PL process. Therefore, both reasons cause discrepancies in the critical distance values. Despite discrepancies in the critical distance values, we could expect that the critical distance value using the critical concentration data was more reasonable than the critical distance value obtained using spectra overlap data.

Nonradiative energy transfer from a Eu$^{2+}$ ion to another Eu$^{2+}$ ion may occur as a result of an exchange interaction, radiation reabsorption, or multipole–multipole interaction. Dexter already reported that exchange interaction is responsible for energy transfer for forbidden transition and typical critical distance, which is about 5 Å. Because, in the case of CMS:Eu$^{2+}$ phosphor, the energy transfer mechanism of Eu$^{2+}$ is the $4f^{7} \rightarrow 4f^{5}5d$ allowed electric–dipole transition, the exchange interaction plays no role in energy transfer between Eu$^{2+}$ ions. Therefore, the process of energy transfer will occur as an electric multipole–multipole interaction according to Dexter theory. The emission intensity ($I$) per activator ion follows the equation given below:

$$ I = \frac{k}{C [1 + \beta C^{\theta/3}]} , \quad (3) $$

where $C$ is the activator concentration involved in self-concentration quenching, $k$ and $\beta$ are constants for each interaction in the same excitation conditions for a given host lattice. For $C \gg X_c$, the non-radiative losses are attributable to multipolar transfer, and for $\beta^{\theta/3} \gg 1$, Eq. (3) can be simplified as shown below

$$ \frac{I}{C} = \frac{k_1}{\beta C^{\theta/3}}, \quad (4) $$

where $k_1$ is a constant. The value of $\theta$ is 6, 8, and 10 are dipole–dipole, dipole–quadrupole, or quadrupole–quadrupole interactions, respectively. The value of $\theta$ can be determined from the slope ($-\theta/3$) of the linear line in Fig. 6, which plots $\log(I/C)$ versus $\log(C)$ on a logarithmic scale of $I/C$. The value of $-\theta/3$ is found to be $-2.00273$. Therefore, the value of $\theta$ is calculated to be approximately 6. This indicates that the dipole–dipole interaction is the concentration quenching mechanism of Eu$^{2+}$ emission in the CMS:Eu$^{2+}$ phosphor.

IV. CONCLUSION

We optimized synthesis conditions of CMS:Eu$^{2+}$ in terms of factors such as activator concentration, gas flow rates, and SiO$_2$ ratios, and successfully determined structure parameters by Rietveld refinement method with neutron powder diffraction data. In addition, we investigated fundamental luminescent properties of the optimized CMS:Eu$^{2+}$. The concentration quenching process is observed, the critical quenching concentration of Eu$^{2+}$ in CMS:Eu$^{2+}$ is about 0.01 mol, and critical transfer distance of 12 Å is obtained. On the other hand, based upon the Rietveld refinement and Dexter theory, the critical transfer distance is calculated as 27 Å. Despite discrepancy in the critical distance values, we could expect...
that the critical distance value using the critical concentration data was more reasonable than the critical distance value obtained using spectra overlap data. As a result of the fitting value between the emission intensity per activator concentration and activator concentration, the dipole–dipole interaction was a dominant energy transfer mechanism of electric multipolar character of CMS:Eu$^{2+}$.

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